



Tutorials and worked examples for simulation,
curve fitting, statistical analysis, and plotting.
<http://www.simfit.org.uk>

Given a model defining one or more equations in one or more variables, the integral(s) can be estimated over a hyper-rectangular region defined by fixed limits.

The following procedure is required for just one function of $m \geq 1$ variables, although $n \geq 1$ functions of $m \geq 1$ variables can be analyzed in exactly the same way.

1. Create a file defining the function of m variables to be integrated.
2. Open program **usermod** and input the file defining one function of m variables.
3. It is necessary to explicitly indicate that one function is required and m must be input correctly.
4. Program **usermod** then checks that the function is defined correctly.
5. The range of integration required must be defined by editing the vectors *BLIM* and *TLIM* to specify the m lower and upper limits for the corresponding variables.
6. The absolute error *EPSABS* and relative error *EPSREL* parameters required must be set.
7. Integration can then be requested but the result should only be accepted if *IFAIL* = 0 on completion.
8. If $|IFAIL| > 0$ some of the previous parameters will have to be adjusted.

From the main SIMFIT menu, choose [A/Z], open program **usermod**, then read in the test file `d01fcf.mod` which defines the integrand used to evaluate the following integral

$$I = \int_0^1 \int_0^1 \int_0^1 \int_0^1 \frac{4u_1u_3^2 \exp(2u_1u_3)}{(1 + u_2 + u_4)^2} du_4 du_3 du_2 du_1$$

and the results are listed in the next table.

<i>IFAIL</i>	0 (from <i>D01EAF</i>)	
<i>EPSABS</i>	1.000E-06	
<i>EPSREL</i>	1.000E-03	
Number	<i>BLIM</i>	<i>TLIM</i>
1	0.0	1.0
2	0.0	1.0
3	0.0	1.0
4	0.0	1.0
Number	<i>INTEGRAL</i>	<i>ABSEST</i>
1	0.57533267	1.0782E-04

Note that in order to perform the integration it may be necessary to re-define the limits, absolute, and relative tolerances, which can be done interactively.

Exit with *IFAIL* = 0 indicates that the absolute error estimate *ABSEST* satisfies

$$|ABSEST| \leq \max(EPSABS, ABSREL \times |INTEGRAL|)$$

as defined for NAG routine *D01EAF*.

The model equation file `d01fcf_e.mod` is as follows.

```
%  
f(y) = {4y(1)y(3)^2[exp(2y(1)y(3))]}/{1 + y(2) + y(4)}^2  
%  
1 equation  
4 variables  
0 parameters  
%  
begin{expression}  
f(1) = 4y(1)y(3)^2[exp(2y(1)y(3))]/[1.0 + y(2) + y(4)]^2  
end{expression}  
%
```